Nanoscale toughening of ultrathin graphene oxide-polymer composites: mechanoochemical insights into hydrogen-bonding/van der Waals interactions, polymer chain alignment, and steric parameters†

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This paper describes a systematic study on the nanoscale toughening of monolayer graphene oxide (GO) by an ultra-thin polymer adlayer, which impedes the propagation of cracks during intraplanar fracture. Using molecular dynamics simulations, the crack-bridging capabilities of a library of five hydrogen-bonding-capable polymers are explored against an epoxide-rich GO substrate. The best crack-bridging effect is found in polymers with functional groups that can both donate/accept hydrogen atoms and have better capability to form cooperative hydrogen bonds. Aligning the chains of poly(acrylic acid) orthogonally to the crack propagation direction significantly enhances the fracture toughness of monolayer GO (by 310%) in comparison to that for an adlayer with randomly arranged chains (180% enhancement). Notably, van der Waals interactions, which are seldom highlighted in the fabrication of strong GO-polymer interfaces, are found to also provide significant crack-bridging capabilities when the polymers possess large side groups. These results pave the way for a set of design criteria that can help in remediating the intrinsically brittle mechanical behavior of two-dimensional materials, a barrier that currently restricts their potential applications.

Introduction

Two-dimensional (2D) materials, with exceptional physical properties derived from sub-nanometer thick well-defined atomic structures, hold enormous promise for the development of next-generation devices, including flexible displays and bio-integrated systems such as flexible electronics.1,2 However, they tend to exhibit an intrinsic brittle behavior,3,4 which raises integrity concerns in large-scale applications where defects and stresses are inevitable. Thus, the exploration of toughening strategies for these 2D materials to overcome their intrinsic mechanical weaknesses has emerged as a critical research frontier in recent years.5 While many chemical insights have been garnered over the past decade,6 a quantitative understanding of the toughening mechanism is still lacking.

Mechanistically, the strategies that have been proposed for toughening 2D materials can be broadly classified as either intrinsic or extrinsic. Intrinsic toughening includes introducing “traps” ahead of a crack tip to retard crack propagation, either through strain-induced functional group transformations7 or by topological defects.8,9 Extrinsic toughening, on the other hand, requires the deposition of a second material to bridge, and thus impede, a propagating crack through strong interfacial adhesion. Among various 2D materials, graphene oxide (GO) is one in which both types of toughening can be deployed due to its rich and versatile surface chemistry. As a functionalized derivative of graphene, GO possesses a plethora of functional groups including hydroxyl, epoxy, and carboxyl,10,11 whose chemical compositions can be tuned at will to afford materials with a broad range of mechanical properties.7,12–17 For example, intrinsic toughening in epoxide-
rich GO can be enabled through an epoxide-to-ether transition that dissipates energy during tensile loading, resulting in a 100% enhancement in toughness in comparison to a hydroxylated GO. Pathways to extrinsic toughening of GO nanosheets have been demonstrated by the incorporation of polymers that can form an extensive network of hydrogen bonds (HBs) with oxygen functional groups. Indeed, GO has been combined with a variety of hydrogen-bonding-capable synthetic and bio-polymer networks such as PVA, PMMA, silk fibers, and chitosan, resulting in macroscopic GO-polymer nanocomposites that are stronger and tougher than GO paper alone. While these earlier experiments are highly inspirational, there is a lack of quantitative knowledge on how polymer properties such as chemical compositions and chain conformations may affect the ability of the polymer layer to hinder a propagating crack. Achieving a better understanding of structure-property relationships would enable the materials engineering community to expand the scope of available GO-based materials beyond the intrinsic toughening of GO itself.

Herein, we report that the fracture toughness of monolayer GO can be increased by 40–180% through the incorporation of an ultra-thin (1.5–4 nm) layer of hydrogen-bonding-capable polymers with the chain randomly distributed on the surface. Up to 310% increase in fracture toughness can be achieved with poly(acrylic acid) if the polymer chains are fully extended and oriented orthogonally against the propagation direction of the crack. This discovery is made possible through a systematic molecular dynamics (MD) study that unravels how the propagation of cracks in a GO nanosheet is impeded by the polymer chains. MD simulations over a small library of hydrogen-bonding-capable polymers enable a comprehensive optimization of the chemical composition, chain conformation, and surface adsorption of the polymer adlayer to allow for the strongest interactions possible with the heterogeneous functional chemistry of the GO sheet, and thus the best fracture toughness. Surprisingly, it reveals that the cohesive bonding between the HB-capable polymer adlayer and the GO surface is also significantly affected by van der Waals (vdW) interactions. Together, these results allow us to establish key design criteria for deploying polymers that can better impede the crack propagation in monolayer GO, suggesting that the range of polymers implemented in GO-polymer nanocomposites can (and should) be extended beyond a selected few that are known to form HBs and π-π-stacking interactions with the GO surface.

Such simulation-driven analysis can eventually be generalized to understand toughening in any functionalized 2D material system that does not have HB capabilities.

### Results and discussion

#### Selection of model systems

Recently, Soler-Crespo et al. reported that an ultra-thin layer of poly(vinyl alcohol) (PVA) adsorbed on epoxide-rich GO (4:1 epoxide/hydroxyl ratio), fabricated using an experimental Langmuir–Blodgett deposition strategy, can significantly enhance the toughness of GO without sacrificing its native 2D modulus. For GO-PVA nanolaminates, AFM-based indentation tests reveal a three-fold enhancement of load-bearing capability and several-fold increase of energy dissipation in comparison to GO nanosheet. Such enhancements were proposed to arise from a crack-bridging mechanism where the propagation of nanoscale cracks can be shielded by the stretching of PVA chains over crack openings that are as large as 10–20 nm. The strong toughening effect by the polymer chains is possible due to their multiple-hydrogen-bond interactions with the surface oxygen groups of the GO sheet. These interactions are maximized due to the synergistic matching of the oxidized domain size of the substrate and the length of the adsorbed polymer chain. A similar crack-bridging scheme has also been proposed for a covalently linked graphene-carbon nanotube system, raising the possibility that a general approach for crack shielding can be proposed for a broad range of materials that interact strongly with a 2D nanosheet. Thus, we hypothesize that a systematic investigation of the interactions between the polymer adlayer and the GO sheet can result in a number of available GO-polymer materials exhibiting extrinsic toughening. We set out to investigate this idea using an epoxide-rich GO nanosheet model that is similar to that used experimentally by Soler-Crespo et al. to favor strong interactions with the hydrogen-bonding-capable polymer adlayer. This in turn will facilitate the comparison of the crack-bridging properties in GO-based nanocomposites by polymers with different chemical and structural features and allow for a clear elucidation of the extrinsic toughening effect from a molecular-level viewpoint.

For model polymers that can form hydrogen bonds with the epoxide-rich GO, we select five oxygen-containing polymers that have often been used in GO-polymer nanocomposites: poly(acrylic acid), poly(methyl acrylate), poly(vinyl alcohol), poly(butyl acrylate), and poly(ethylene glycol) (abbreviated as PAA, PMA, PVA, PBA, and PEG, respectively). This polymer library (Fig. 1) allows for full coverage of the two key factors that affect HB formation between these oxygen-containing polymers and the surface oxygen species of GO: the types of HB species and the “length” of the side group. The three main types of HB species (carboxyl, hydroxyl and ether functional groups) are studied by comparing PAA, PMA, PVA, and PEG. Notably, the critical effect of having both HB donor/acceptor in the same polymer is elucidated in the series of two homologous carboxylated polymers (PAA, PMA), with PAA being able to both donate and accept hydrogen atoms (HB donor/acceptor) while PMA only capable of accepting hydrogen atoms (HB acceptor). Comparing PMA to PBA reveals the effect of the side group length. Moreover, the contribution to toughening from vdw interactions increases for PMA and PBA, which allows us to contrast the toughening effect from HBs with that from vdw interactions.

To be consistent with the GO-PVA experimental system reported by Soler-Crespo et al., we employ a 134-repeating unit (degree of polymerization (DP) = 134) PVA chain and a final polymer thickness of ~1.5 nm. This is equivalent to
6 polymer chains for a 7.5 × 7.1 nm² GO sheet and ∼48 wt% PVA composition. The number of the polymer chains (6) and polymer length (DP = 134) are maintained for the GO-polymer models (PAA, PMA, and PBA), which have 2 C in each repeating unit in the backbone. For PEG, which has 2 C and 1 O in each backbone repeating unit, a polymer chain of equivalent length (DP = 90) is chosen but the number of polymer chain/GO sheet is still maintained at 6.

Adsorption of polymer chains on GO

To explore the toughening effects of polymer adlayers as they would exist in a composite material, we configured our model system as a mixture of GO and polymer melts. Following the approach described in Auhl et al.,26 we generated polymer chains with melt-state conformations (see ESI, Section S1†) and maintained their melt-state statistics until they were adsorbed onto the GO surface. After contact, the whole system was kept above the glass-transition temperature of the polymers until the total energy converges to a minimum (see Experimental section). The crack-bridging simulation was then performed after this annealing process. Drawing an analogy from the bridging of cracks in fiber composites, which is controlled by the fiber conformation (embedded length, orientation, etc.),27 we hypothesize that the extrinsic toughening, or the crack-bridging effect, in our GO-polymer models would be similarly governed by the nanoscale conformation of polymer chains (end-to-end distance and orientation). However, as our vinyl polymer chains are “flexible” on a molecular scale, they can form a multitude of intra- and inter-chains interactions that greatly reduce their end-to-end distance in comparison to their contour lengths (i.e., the length of the polymer at maximum physically possible extension).28 This in turn will affect the crack-bridging properties of a polymer chain at the nanoscale as its fully extended conformation across a crack is expected to impede the propagation of that crack better than a coiled up one.

Fig. 2a shows the physical probability curves for finding an atom from the adsorbed polymer chains at a given height or distance (D) from the basal plane of the GO sheet. These number-density profiles all have a peak at ∼0.45 nm, representing atoms that are in direct contact with the GO sheet, or in other words, “closely adsorbed”. As the side group of the polymer becomes larger, the proportion of these closely adsorbed atoms decreases, from 0.22 for PEG to 0.04 for PBA. At the same time, the thickness of the polymer adlayer increases, from 1.55 nm for PEG to 4.45 nm for PBA. A second peak at ∼1 nm, arising from the non-bonded neighbors of the closely adsorbed atoms, is also visible in the number-density profiles but becomes less obvious with increased side group size, again consistent with the decreased proportion of close-adsorbed atoms. To characterize the extent that the backbone of a polymer chain associates with a...
surface, we employ the orientation-order parameter $P_2(\phi)$, which is calculated as:

$$P_2(\phi) = \frac{1}{2} \langle 3 \cos^2 \phi - 1 \rangle$$  \hspace{1cm} (1)

where $\phi$ is the angle between the vector that is normal to the surface (i.e., the z-axis, Fig. 3a) and the backbone bonds of the adsorbed polymer chains. Good adsorption occurs when all the backbone bonds are parallel to the adsorbed surface, resulting in $P_2(\phi) = -0.5$ ($P_2(\phi) = 1$ when all the backbone bonds are perpendicular to the surface, and $P_2(\phi) = 0$ when the backbone bonds adopt random orientations). Fig. 2b shows the plots of $P_2(\phi)$ for the five polymers in this study at various distances $D$ from the GO surface. Consistent with the ultrathin nature of the polymer adlayer, the $P_2(\phi)$ plots for all five GO-polymer models exhibit a minimum negative value at $\approx 0.45$ nm, the distance of the closely adsorbed backbone atoms.

Crack-opening simulations

To quantify the toughening effect of the various polymers investigated herein, we implement Rice’s $J$-integral approach, which captures non-linear crack-tip-toughening processes that occur in materials that do not behave in an elastic fashion, as have been observed for GO nanosheets.\textsuperscript{7,17} As well-known in the literature for fiber-reinforced composites,\textsuperscript{27,32,33} the presence of a small amount of reinforcing fibers in a material can greatly enhance its ability to resist the propagation of developing cracks. The presence of fibers effectively allows for the development of a process zone (i.e., the region of space surrounding the crack tip) whose size is not negligible compared to the crack length, thus invalidating the fundamental assumption of linear-elastic fracture mechanics. In the case of macroscopic fiber-reinforced composites, bridging fibers can effectively resist the extension of a large crack by dissipating a significant amount of energy through the decohesion of the fiber-matrix interface.\textsuperscript{32} We thus envision that a similar mechanism will arise in the GO-polymer systems examined in this work where the polymer chains can bridge an extending crack, by anchoring to the GO sheet through HBs.

Unlike many brittle materials whose fracture energy can be characterized solely by a single number $G_b$, the critical energy release rate, the resistance of polymer-toughened GO composites must be described by a resistance ($R$) curve (see ESI, Fig. S1f), whose steady-state value can be estimated by calculating the 2D energy release per unit distance following the established $J$-integral approach for a fiber-reinforced system:\textsuperscript{27,32,33}

$$G_c = J_c = G_b = G_t = G_0 + \int_0^{\delta_c} T(\delta)d\delta$$  \hspace{1cm} (2)

where $G_c$ is the critical energy release rate (expressed in energy/distance unit) of the composite, $G_t$ is the energy release rate due to bridging, $T$ is the traction between the crack surface, and $\delta_c$ is the size of the critical crack-opening after

Fig. 3 Plots of the GO-PAA simulated configurations. Carbon atoms are colored grey, oxygen atoms are colored red, and hydrogen atoms are colored white. To contrast with the polymer, the GO molecules have been reduced in their relative sizes. When the simulation comprises multiple polymer chains, as in panels (a) and (b), one representative polymer chain is highlighted in yellow to enhance visualization. (a) A crack-opening simulation where polymer chains are randomly adsorbed on a pre-cracked GO prior to its opening. Our model comprises six 134-repeating unit polymer chains adsorbed on a 7.5 × 7.1 nm² GO sheet and a final polymer thickness of ~1.5 nm (~60 wt% PAA). The number of polymer chains (6) and polymer length (DP = 134) were maintained for all the four GO-vinyl-functionalized polymer models (PAA, PMA, PBA, and PVA), which have 2 C in each repeating unit in the backbone. For PEG, which has 2 C and 1 O in each backbone repeating unit, the equivalent polymer was chosen as a chain with DP = 90 but the number of polymer chains/GO sheet was still maintained at 6. The 2D traction ($T_{2D}$) was recorded as a function of the crack-opening ($\delta$). (b) An ideal crack-opening scenario with all six polymer chains extend close to their contour length and are aligned orthogonally to the crack-propagation direction. (c) A single-chain pull-off simulation where a single polymer chain (DP = 40 for vinyl polymer models, and DP = 27 for PEG) is pulled off from the surface of GO with a spring force at a constant velocity. The pulling force ($F$) and the displacement ($d$) of the carbon atom being pulled along the x-direction were recorded in the simulations.
which $T$ vanishes. As described in the ESI, Section S2, $G_c$ is calculated by super-imposing $G_0$ (the critical energy release rate of GO, found to be 4 nJ m$^{-1}$ for GO monolayers as the average of a hydroxyl-rich GO (3.4 nJ m$^{-1}$) and an epoxide-rich GO (4.6 nJ m$^{-1}$)34) and the energy dissipation from the polymer $G_c$. As the value of $G_0$ implicitly “contains” information for an already initiated crack,33 we can investigate the non-linear effects of polymer toughening in GO by examining the process of crack-opening (i.e., behind the crack tip).

We note that while eqn (2) is derived for a continuum system with a homogeneous distribution of masses, the fact that we use discrete molecular models, in the MD simulations, does not prevent utilization of eqn (2) in view that the molecular models are simply used as representative volume elements (RVEs) to estimate the behavior of the material in the energy-dominated regime, where the crack size is much larger than their dimensions. At such a scale difference, local mass fluctuations caused by non-uniform distributions of polymer chains are negligible and the entire system is considered “homogenized”.

Fig. 3a shows the schematic of the crack-opening simulation, which involves multiple polymer chains that were randomly adsorbed on a pre-cracked GO sheet (see ESI, Video 1† for a movie of the polymer chain motions). We calculated the crack-bridging force provided by the polymer and then divided the force by the width of GO (the $y$ dimension in Fig. 3a) to obtain the 2D traction ($T_{2D}$) as a function of the crack opening ($\delta$) (see Fig. 4a and ESI, Section S3†). As expected, $T_{2D}$ decreases as the crack-bridging chains are being pulled off from the GO surface and their stick-slip motions can be observed as irregular “peak-valley” patterns along the diminishing traction profile. To quantify the crack-bridging effect, we calculated the 2D energy release rate $G_t$ (Fig. 4b, see also ESI, Table S2† for the full datasets) for all polymers by integrating the areas under the $T_{2D}$ profiles (Fig. 4a and ESI, Section S3†). From this data, the enhancement in GO-fracture toughness due to the polymer crack-bridging effect ($\frac{(G_c - G_0)}{G_0}$ which is $G_t/G_0$), is 40–180% (Fig. 4c), comparable to that observed experimentally (up to 200%) for an ultrathin GO-PVA nanocomposite.33

As shown in Fig. 4b, the crack-bridging performances of the four vinyl-functionalized polymers (PAA, PMA, PVA and PBA) randomly adsorbed on GO, as represented by the blue bars, are better than that for PEG, albeit with large standard deviations that can partially be attributed to the discrepancy between the large number of possible starting conformations by the six polymer chains in this system (an ideal conformation will be described in the next paragraph) and the limited number of possible replica simulations. Nevertheless, assuming that $G_t$ follows a Gaussian distribution, we used the Student’s $t$-distribution to compare the $G_t$ values between pairs of polymers to elucidate the toughening effect by the different types of HB species and the length of the side group. At 95% level of confidence, such analysis reveals that the $G_t$ of PAA is larger than those of PMA ($p$-value$^{35} = 0.042$) and PVA ($p$-value = 0.048). However, the suggestion that the $G_t$ of PAA is larger than that of PBA, which in turn is larger than the $G_t$ of PMA, can only be made at $\sim$80% level of confidence.

To better quantify the crack-bridging effect of each of the five polymers in this study, we reduced the large number of possible starting conformations for the nanocomposite down to an ideal crack-bridging scenario where all of the polymer chains were adsorbed onto the GO surface at their contour length and were aligned orthogonal to the crack propagation direction, as shown in Fig. 3b. These systems were then equilibrated following the same procedure used for the random conformation case. We further constrained the simulation to have all chains being simultaneously pulled off from the same side of the crack. The obtained $G_t$ values for the five models in this idealized scenario, represented as green bars in Fig. 4b, are consistently much higher than those for the randomly adsorbed case (blue bars in Fig. 4b). Notably, the $G_t$ value for the PAA provided the best crack-bridging effect, with 310% enhancement (Fig. 4c) in fracture toughness! While not directly comparable, this value is very similar to that recently

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**Fig. 4** Results of the crack-opening simulations. (a) A typical 2D traction ($T_{2D}$) – crack opening ($\delta$) curve of a GO-PAA system. (b) 2D energy release rate $G_t$ for the GO and GO-polymer systems. $G_0$ represents the 2D energy release rate of GO itself. $G_t$ values were calculated by numerically integrating the $T_{2D}$ – $\delta$ curve for all polymers. The blue bars are $G_t$ values of the polymers with random chain arrangements (Fig. 3a). The sample standard deviations were calculated from six simulations (ESI, Section S6†). The green bars correspond to cases where all polymer chains are aligned orthogonal to the crack propagation direction and contribute to the crack-bridging (Fig. 3b). (c) Enhancement of the fracture toughness of GO from the adsorbed polymers with aligned and random chain conformations. The enhancement was calculated as $G_t/G_0$. The average $G_t$ values were used for the random cases.
modeled for the covalently linked graphene-CNT system,\(^\text{22}\) (360% enhancement in energy release rate with completely aligned CNT arrays), suggesting that excellent extrinsic toughen-
ing in GO-based nanocomposites can indeed be achieved with ultrathin soft polymer adlayers as long as strong chemical
interactions can be engineered into the system. Notably, the optimal \(G_1\) values for these ideal crack-bridging simulations
have a strong positive correlation with the average \(G_1\) of the aforementioned randomly adsorbed GO-polymer models (cor-
relation coefficient of 0.9848), allowing us to increase the level of confidence in the latter set of data, and conclude that the
effect of PAA > PBA > PVA > PMA > PEG in crack-bridging. As experiments that can verify such a relationship would require
an enormous amount of effort in both fabrication and measurement of the types recently reported,\(^\text{33,36}\) our MD predic-
tions can serve as a facile pre-screen prior to the more expensive and time-consuming experimental phase.

In addition to the fracture energy, nanoscale fracture has also been proposed to be governed by a “characteristic size” or
flaw-tolerance phenomenon,\(^\text{32,36}\) which can potentially be modified by the polymer adlayer. In our estimation, the pres-
ence of the polymer adlayer should have a minimal effect on the intrinsic characteristic size of the GO sheet. Indeed, when
the defect size is smaller than the characteristic size, where the strength of the material controls failure, the absorbed un-
stretched polymer chains, which have a much lower stiffness than GO, would have a negligible contribution to relieving
the stress concentration in GO and thus are not expected to affect its characteristic size. On the other hand, for defects that are
larger than the characteristic size, in the energy-dominated regime, the adlayer can provide an extrinsic toughening to GO,
as shown herein. In essence, while the polymer adlayer does not prevent crack initiation from defects, it does contribute to
resisting its growth.

**Single-chain pull-off simulations**

To understand the aforementioned trend in crack-bridging simulations in terms of HB donor/acceptor effect, the length of
the side groups, and the type of HB species, we carried out single-chain pull-off simulations (Fig. 3c) for each of the
adsorbed polymer model, starting from the ideal crack-bridging configuration of the polymer chain being orthogonal to
the propagation direction to the crack. To reduce the computational cost and increase the statistical accuracy, we decreased
the system size (the polymer length was shortened to \(\sim 1/3\) and the GO area was reduced by \(\sim 1/2\)) and assumed a con-
figuration where each polymer chain initially resided on one side of the crack. The polymer was then pulled off from this
one side, essentially constraining the polymer motion to only “one GO surface”. In this configuration, all polymer chains
started with similar contour length and followed similar motion paths, so the difference in their cohesive behaviours
can be solely attributed to the chemical properties of the polymer. Following an approach that was applied to simulate
the motion of hydrogen-bonding-capable polypeptides on hydroxylated substrates,\(^\text{37}\) the polymer chain was pulled off the
GO surface with a spring force \((F)\) at a constant velocity (Fig. 3c). During the pull-off simulations, we measured \(F\) as a
function of the displacement \((d)\) of the polymer carbon atom to which the spring was connected. Since we pulled the chain
off at a constant velocity, the spring force varied as a function of the instantaneous GO-polymer interactions, allowing
for the “detection” of stick-slip motions that were proportional to the magnitude of the interaction energy with the GO
surface.

As shown in Fig. 5a, the \(F-d\) curve for the GO-PAA system clearly displays a jagged sawtooth pattern that is indicative of
the expected stick-slip behaviour for a PAA chain that forms multiple HBs with the GO surface (see ESI, Video 2,\(^\dagger\) for
the movie of this simulation). As the pulling initiates, multiple HBs serve as anchoring points to the GO surface, causing
the PAA chain backbone to stretch and giving rise to local increases of the pulling force (stick stages). Rupturing these
HBs releases the stored elastic energy and leads to a sudden drop in the pulling force (slip stage), where interfacial sliding
occurs. After this slip, HBs quickly realign between the GO surface and the next repeating unit of the PAA chain, building
up to the next rupture/slip event and ultimately resulting in several stick-slip transitions throughout the polymer pull-off
process. As the values for \(F\) and \(d\) of the stick-slip events are larger than those for the rupture of a single hydrogen bond,
each slip event must involve the rupture of HBs in a cluster fashion.\(^\text{38}\) The average number of HBs that rupture in such a
cluster can then be estimated from the release of elastic energy,\(^\text{38}\) as shown below (see Evaluation of chemical effects in
the single chain pull-off simulations section).

Fig. 5a shows a gradual decrease in the pulling force as the polymer chain in our PAA-GO model is pulled off the GO
surface, not surprisingly, due to the decrease in polymer-GO interactions. Normalizing this force by the number of repeating
units \((N)\) that are instantaneously adsorbed on the surface of GO shows that the per-repeating-unit force \((F/N)\) remains at
a steady-state value of \(0.045 \pm 0.004\) nN (red line in Fig. 5b; see ESI, Section S4\(^\dagger\) for the other \(F-d\) profiles) up to a displace-
ment of 5 nm \((\sim 1/2\) of the initial polymer length), suggesting that it can be used to represent the average force that each
repeating unit of the polymer chain “exerts” on the GO surface when the opening of the crack is \(\leq 1/2\) the length of the polymer
chain. As such, this average \(F/N\) value can be correlated to the strength of interactions between each repeating unit of the
PAA chain with the GO surface, and thus its overall crack-bridging behaviour.

Indeed, the trend in \(F/N\) data (Fig. 5c) for all of our poly-
mers tracks quite well with the trend in the molar per-repeat-
ing-unit binding energy \(E/N\), suggesting that the pulling force exerted on the GO surface by each type of polymer can be
understood in terms of the chemical interactions as parameterized by the MD force fields.\(^\text{39}\) Additionally, as \(E/N\) can be
decomposed into Lennard-Jones (LJ) and Coulombic (Coul) energies, the strength of the interactions between each
polymer chain and the GO surface can be further quantified in terms of vDW and HB interactions,\(^\text{40}\) respectively (Fig. 5d).
Comparison between the multi-chain crack-opening and single-chain pull-off simulations

While the single-chain pull-off simulations can be considered simplified snapshots of the multi-chain crack-opening simulations, the PBA > PAA > PMA > PVA > PEG trend in \( F/N \) data (Fig. 5c) does not quantitatively agree with the PAA > PBA > PVA > PMA > PEG trend in \( G_t \) data (Fig. 4b). Together with the larger-than-Coulombic LJ contributions to \( E/N \) data found for PBA and PMA (Fig. 5d), this discrepancy highlights the significant capability of vdW interactions to provide good crack-toughening interfaces. Taken one step further, this observation suggests that the scope of polymer adlayers that can toughen GO-polymer nanocomposites can (and should) be extended to include polymers that have good vdW interactions with the GO surface in addition to the few that were historically chosen due to their perceived abilities to form strong HBs and \( \pi-\pi \)-stacking interactions with GO.\(^6\) For example, our work herein clearly shows that replacing the carboxyl groups in PAA with the carboxymethyl group in PMA can increase the LJ contribution to \( E/N \) to exceed the Coul component (Fig. 5d). Further increase of the size of the ester group to a larger carboxybutyl group, as in PBA, increases the LJ contribution to \( E/N \) to almost twice that of the Coul component, and this leads to the \( F/N \) value for PBA being comparable to PAA in the single-chain pull-off simulation. Supporting this notion is the recent report that polydimethylsiloxane (PDMS), which primarily interacts with GO through vdW interactions, significantly enhances the toughness and stiffness of graphene-based nanocomposites in comparison to GO foam (28 \( \times \) higher toughness and 65 \( \times \) higher stiffness with 1.5 wt% of PDMS).\(^{41,42}\)

Interestingly, while the \( G_t \) value of PVA is almost twice that of PEG in the multi-chain crack-opening simulation (Fig. 4b), its \( F/N \) value is quite similar to that of PEG in the single-chain pull-off simulation (Fig. 5c). Given the identical atomic composition between these two polymers (repeating units = \( \text{C}_2\text{H}_4\text{O} \)) and the better “packing” of the PEG chains on the GO surface (Fig. 2a), this inconsistency can only be attributed to the additional crack-bridging effect from a network of hydrogen-bonded polymer chains produced by inter-chain HBs in the GO-PVA case, as has been proposed to explain experimentally measured crack-toughening.\(^{6,41}\) This is akin to the case of fiber-reinforcement of concrete where a network of “crack-bridging” struts can lead to vast improvements in the ability of the matrix to impede crack propagation.

That PBA and PAA both have similar \( F/N \) values in the single-chain pull-off simulations (Fig. 5c) but large differences in \( G_t \) data in the multi-chain crack-opening simulations (Fig. 4b) further indicates a clear reduction in the ability of a
randomly distributed multi-chain PBA film to bridge a developing crack in comparison to PAA. This is presumably due to a reduction of GO-polymer interactions: the large carboxybutyl side groups of the PBA chains do not allow them to pack in the adlayer in a manner that maintains the most optimal interactions between each polymer chain and the GO surface, as confirmed by the lower proportion of closely absorbed atoms for PBA when multiple chains are present (Fig. 2a). In such a situation, polymer-polymer inter-chain vDW interactions presumably increase at the expense of GO-polymer interactions. In the next section, we will make an attempt to quantify the relationship between chemical effects, such as the types of hydrogen bonds and their number, and the crack-toughening mechanism.

Evaluation of chemical effects in single chain pull-off simulations

The per-repeating-unit strength of the HB interaction that our five polymers make to the GO surface can also be obtained from the single-chain pull-off simulations as the dimensionless quantity \( N_{HB}/N \) (Fig. 6a; see Experimental section and ESI, Section S5† for \( N_{HB}/N \) datasets). This value allows us to separate our five models into two classes: those that can only accept hydrogen atoms (PMA, PBA, and PEG) and those that can both accept and donate hydrogen atoms (PAA and PVA).

Notably, comparing PAA and PMA, whose carboxyl side groups are roughly of the same size, offers clear insights into how these different HB capabilities are translated into very different Coul contributions. With its carboxyl groups capable of both donating and accepting HBs, PAA can form more HBs with our epoxide-rich GO surface (epoxide groups are HB acceptors) in comparison to PMA (Fig. 6a), resulting in a higher Coul contribution (Fig. 5d, cf. Coul energies). Although the methoxy groups of PMA do provide some vDW interactions, the accompanying energy gain (Fig. 5d, cf. LJ energies) does not adequately compensate for the loss of HB interactions, thus yielding lower overall \( E/N \) and \( F/N \) data (Fig. 5c). Such a comparison clearly indicates the advantage that polymers with both HB donors and acceptors have over those with only HB acceptors in providing stronger interface with the GO sheet and thus better mechanical performance for the corresponding GO-polymer composite. This conclusion is consistent with that reported in a previous experimental study,† where GO-PVA nanocomposites show better mechanical properties than GO-poly(methyl methacrylate) nanocomposites because the latter polymer adlayer is only capable of accepting hydrogen atoms.

Interestingly, while PVA shows an \( N_{HB}/N \) value that is 570% higher than that for PEG, this difference only manifests in \( \sim 29\% \) increase in \( F/N \). In contrast, PAA, which has the same \( N_{HB}/N \) value as PVA but with one more “CO” in its side group, shows almost 100% increase in \( F/N \) value than PEG. This difference can be explained by the better ability of PAA to form a cooperative HB pair with the epoxide-rich GO surface using just one repeating unit in the polymer chain (Fig. 6b). This is in contrast to PVA, which requires two adjacent repeating units to form such a pair (Fig. 6b). In other words, a single carboxyl group in a PAA repeating unit can form a cooperative HB pair (or participate in larger cooperative HB clusters) that would be broken in concerts in a pull-off experiment,† resulting in a stick-slip motion that has larger \( F \) and \( d \) values than those for the rupture of a single hydrogen bond. A similar stick-slip event in the GO-PVA model would require two hydroxyl groups from adjacent repeating units, leading to fewer possibilities for stick-slip transitions. Indeed, a rupture strength analysis† (see Experimental section) reveals that one stick-slip motion in PAA requires the cleavage of \( \sim 4 \) hydrogen bonds (vs. 3 for PVA; see Fig. 6c and ESI, Section S5†), resulting in a higher friction force observed for PAA. This finding is also consistent with the report that incorporating carboxyl-functionalized multi-walled carbon nanotubes (MWCNT) into polymer-MWCNT composites can lead to better mechanical properties than hydroxyl-functionalized MWCNT.45

Fig. 6 HB analysis in the single-chain pull-off simulations (a) The number of HBs observed between the polymer chain and GO normalized by \( N \) \( (N_{HB}/N) \) for all five polymer models. HBs were count with a criterion of donor–acceptor distance <3.5 Å and H-acceptor-donor angle <30°,† and were count up to 5 nm displacement. The error bars represent sample standard deviations that were calculated over five replicates of simulations. (b) Illustration (left) and simulation snapshots (right) of cooperative HBs formed at the interface in the PAA and PVA system. For PAA, a cooperative HB pair can form within one repeating unit, where the carbonyl oxygen and hydroxyl group each forms a hydrogen bond, as shown by the blue and red dashed lines, respectively. For PVA, two repeating units are required to form a cooperative HB pair, where one hydrogen bond forms in each repeating unit. In the snapshots, carbon atoms are colored grey, oxygen atoms are colored pink, and hydrogen atoms are colored white. (c) Number of hydrogen bonds \( (N_{H}) \) that are cleaved in a single stick-slip motion for PAA and PVA.
Conclusions

In summary, we have shown that the presence of an ultra-thin adlayer of oxygen-containing hydrogen-bonding-capable polymers on a monolayer epoxide-rich GO can greatly enhance the fracture toughness of this monolayer. With random chain arrangements, the largest enhancement (180%) is found for PAA, whose carboxylate side groups intrinsically place an HB-donor and HB-acceptor moiety close in space, facilitating the formation of cooperative HB clusters that synergistically enhance the interaction of the polymer with the GO surface. The breaking of cooperative HB clusters manifests into stick-slip motions of polymer chains with friction-force magnitudes that are several times larger than the breakage of a single HB. The enhancement further improves to 310% when the PAA chains are orthogonally aligned to the crack propagation direction in the GO. For PMA and PBA whose carboxylate ester groups are only HB acceptors, the enhancements are slightly inferior to that of PAA but are still in an impressive 175–243% range with orthogonally aligned polymer chains. Our MD analysis clearly captures an increase in the overall LJ contribution from these polymers as a function of the length of their side groups. While this vdW contribution can potentially be restricted by the limited packing efficiency, which manifests as larger polymer thicknesses in PMA and PBA, it contributes significantly to the crack-bridging properties, resulting in non-negligible fracture toughness enhancements. Notably, a fully aligned polyethylene (PE, DP = 134) adlayer with the same steric properties as PEG but without the ability for HB formations, can result in an 83% enhancement of GO fracture toughness (ESI, Table S2†), highlighting the importance of vdW interactions.46

Our data strongly advocate three design criteria for rendering ultrathin GO-polymer nanocomposites that are resistant toward nanoscale cracks: (1) maximizing the formation of cooperative HB clusters between the polymer adlayer and the GO surface; (2) aligning the polymer chains orthogonally to the crack propagation direction; and (3) increasing the vdW interactions for polymers that do not have both HB-donors and -acceptors. For GO, these criteria suggest that the range of polymers implemented for GO-polymer nanocomposites should be extended beyond a selected few that are known to form HBs and π-π stacking interactions with the GO surface.6 Most importantly, the last criterion opens up the possibility for toughening a broad range of 2D materials that do not have HB-forming capabilities.

We note in passing that while GO has reduced modulus and strength with respect to graphene7 due to the presence of functional groups on its basal plane, these groups can actually render GO more damage-tolerant through an intrinsic toughening mechanism.7 In addition, they provide possibilities for extrinsic toughening of the GO sheet through interactions with polymer adlayers as shown in this work. By applying a bottom-up materials-by-design strategy, one should be able to optimize the functional-group compositions of GO as well as their spatial distributions to maximize desirable mechanical properties for a particular GO-polymer system. Such investigation can provide important insights into the design of next-generation strong and tough composites.

Lastly, we note that as our current study was primarily aimed to unravel the chemical basis for nanoscale toughening by a polymer adlayer, we did not consider process-related conditions (degree of thermoset cure, polymer chain mobility and crystallinity etc.) and/or mixed-mode phenomenon (e.g., the deflection of the crack propagation due to the adsorbed polymers). While these have been known to affect fracture toughness, their complexity necessitates the consideration of larger model systems and more sophisticated force fields, which would render the computations significantly more expensive.22

Experimental section

General considerations

The simulations were performed on the Stampede2 cluster at the Texas Advanced Computing Center (TACC), University of Texas at Austin, and the Quest cluster at Northwestern University. The CHARMM general force field (CGenFF)47 was used to model the GO-polymer system. The atomic charges and force field parameters for bonded interactions of polymer molecules were obtained from the CGenFF program (interface version 1.0.0, force field version 3.0.1)48 by uploading training structures of each polymer with 10 repeating units. The Lennard-Jones parameters for polymers were obtained from CGenFF C36 version.49,50 The force field parameters for GO were taken from Fonseca et al.50 GO flakes were generated by a Monte Carlo Algorithm described in an earlier work51 with seventy percent of the carbon atoms oxidized and a 4-to-1 epoxide-to-hydroxyl group ratio. Polymer chains were generated by a self-avoiding random walk method. The Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS) software package51 was used to run MD simulations. The timestep was set to be 1 fs, and the inner and outer cutoff distances for non-bonded interactions were set to be 10 and 12 Angstroms, respectively.

Crack-opening simulations

For these simulations, a pre-cracked GO flake with dimensions measuring 7.5 × 7.1 nm was created by cleaving the GO plane along the armchair or zigzag direction of GO and separating the cleaved surfaces by 2 Å. Six atactic polymer chains with their average mean-square end-to-end distance corresponding to their melt states (detailed in ESI, Section S1†) were suspended over the GO flake. The contour length was kept to be 32.5 nm for all polymers (90 repeating units for PEG and 134 repeating units for all the other polymers). The GO flake is large enough to adsorb a polymer chain without affecting its end-to-end distance. Periodic boundary conditions were applied in all directions with a ∼9 nm vacuum above and below the GO-polymer system in the z-direction. To facilitate the polymer adsorption, the polymer chains were pushed against the GO with a potential wall at 650 K for 0.1 ns, during
which the polymer chains interacted via a soft repulsive potential to maintain their melt-state statistics. Upon contact with the surface, the potential wall was removed, and the normal potential was re-established. This process simulated an idealized melt-spinning of polymer on GO where the polymer chains were not affected by solvation and the polymer contour length was maximized against phase separation or intramolecular interactions.

After energy minimization using the steepest descent algorithm, the system was kept at 650 K under an NVT ensemble for 4 to 8 ns (the time to achieve energy convergence varies between polymers) and then annealed to 300 K for 1 ns. During the equilibration, the motion of GO atoms was restricted with a soft spring in all directions to avoid rigid body motion. After equilibration, the simulation box was deformed in the direction perpendicular (in-plane) to the crack with a strain rate of $10^9$ s$^{-1}$. We note that while this strain rate is unrealistic in comparison to what can be achieved in experiments, it can ensure convergence as shown by a previously reported sensitivity analysis$^{21}$ as well as one performed in this work (see ESI, Section S3†). Only the coordinates of GO atoms were mapped into the new box to avoid artificial stretching of the polymer phase. The stress (with a unit of stress × volume) in the polymer phase was calculated by summing the per-atom virial stresses of all polymer atoms. Then, it was divided by the $x$ dimension of the box (see Fig. 3a) to calculate the crack-bridging force and then divided by the $y$ dimension of the box to calculate 2D Traction ($T_{2D}$, with a unit of force/length). A moving average filter of 20 steps was applied to smooth $T_{2D}$. A total of six simulations (three with the pre-crack along the armchair direction and three along the zigzag direction) were performed for each polymer, in which the location of the crack was changed while keeping the same initial polymer configuration, thus providing different polymer configurations over the crack.

**Single-chain pull-off simulations**

For these simulations, one chain at its contour length was adsorbed onto an $11 \times 3.2$ nm$^2$ GO flake. The contour length was kept to be 9.7 nm for all polymers (27 repeating units for PEG and 40 for all other polymers). Periodic boundary conditions were applied in the $y$-direction (see Fig. 3c). The system was equilibrated in an NVT ensemble at 300 K for 1 ns, during which the out-of-plane undulation of GO was restricted by applying spring supports in the $y$- and $z$-axes. The steered molecular dynamics (SMD) method was used to pull the backbone carbon atom at the terminal group with a spring with a spring constant of 100 kcal per mol per Angstrom at a constant velocity of $3.8$ m s$^{-1}$, during which the pulling force ($F$) and the displacement of the carbon atom ($d$) were measured. The pulling velocity was consistent with the strain rate used in the crack opening simulations, and was slow enough for the HBs to reform after a stick-slip event. Throughout the simulation, the rigid body motion of GO was restricted by applying spring supports. A total of five simulations were performed for each polymer in which different initial velocities for atoms were generated. The HBs between the polymer and GO were counted with a criterion of donor–acceptor distance <3.5 Å and H-acceptor-donor angle <30°.$^{44}$ The $N_{HB}/N$ values were calculated by dividing the total number of simulation-observable HBs that the polymer chain made with the GO surface by the number of monomers on the surface of GO ($N$) at the corresponding timestep. To compare the crack-bridging effects in HB-dominated PAA- and PVA-GO models, we adopted a methodology that was used to study the collective effect of HBs on rupture strength in HB assemblies.$^{58}$ We simulated two deformation modes of polymers on GO: out-of-plane peeling and in-plane shear (same as the single-chain pull-off) (ESI, Fig. S4†). In the peeling mode, HBs were cleaved sequentially (i.e., one by one) from the GO surface; however, multiple HBs can be cleaved simultaneously in the shear mode in one stick-slip motion. We found the average rupture force of one cleavage (peeling mode) and one stick-slip motion (shear mode) (see ESI, Section S5†), and calculated the ratio of the average force in the shear and peeling mode ($N_c$), which revealed how many HBs were cleaved simultaneously in one stick-slip motion. Visualization and post-analysis of the system were accomplished with OVITO.$^{52}$

**Conflicts of interest**

The authors claim no conflict of interests.

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**Notes and references**


14 C. Cao, M. Daly, C. V. Singh, Y. Sun and T. Filletre, **Carbon**, 2015, **81**, 497–504.


